



ST. ANNE'S

COLLEGE OF ENGINEERING AND TECHNOLOGY

(Approved by AICTE New Delhi, Affiliated to Anna University, Chennai)

(An ISO 9001:2015 Certified Institution)

ANGUCHETTYPLAYAM, PANRUTI – 607 106.

QUESTIONS BANK

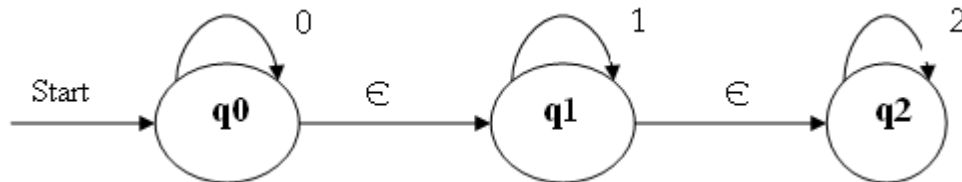
CS8501-THEORY OF COMPUTATION

UNIT-1

FINITE AUTOMATA

PART-A

1. What is a finite automaton? (Nov/Dec 2015)
2. What are the Applications of Automata theory? [May – 2008]
3. What is Induction principle? Give an example. [NOV/DEC 2012]
4. Draw a non-deterministic automata to accept strings containing the substring 0101. (may-2016)
5. State the pumping lemma for regular languages. (may/June 2016)
6. Write Regular Expression for the set of strings over $\{0,1\}$ that have atleast one.(NOV/DEC-2015)
7. What is meant by DFA? [MAY/JUNE 2013]
8. What is a Non-Deterministic Finite Automaton (NFA)? (Nov/Dec 2013)
9. Obtain the ϵ closure of states q_0 and q_1 in the following NFA with ϵ transition?[Dec 2014]



10. Define NFA with ϵ transition. [MAY/JUNE 2013] [APR/MAY 2018]
11. Difference between DFA and NFA.
12. What is a Regular Expression? [NOV/DEC 2012].
13. What are the applications of pumping lemma? [NOV/DEC 2007]
14. Construct a DFA for the regular expression aa^*bb^* .
15. What is $\{10,11\}^*$?
16. Construct NFA for regular expression a^*b^* .
17. Construct a DFA that will accept strings on $\{a,b\}$ where the number of b's divisible by 3.
18. Differentiate L^* and L^+ .
19. Construct the DFA that accepts input string of 0's and 1's not containing 101 as substring. [APR/MAY 2018]
20. Differentiate regular expression and regular language.

PART-B

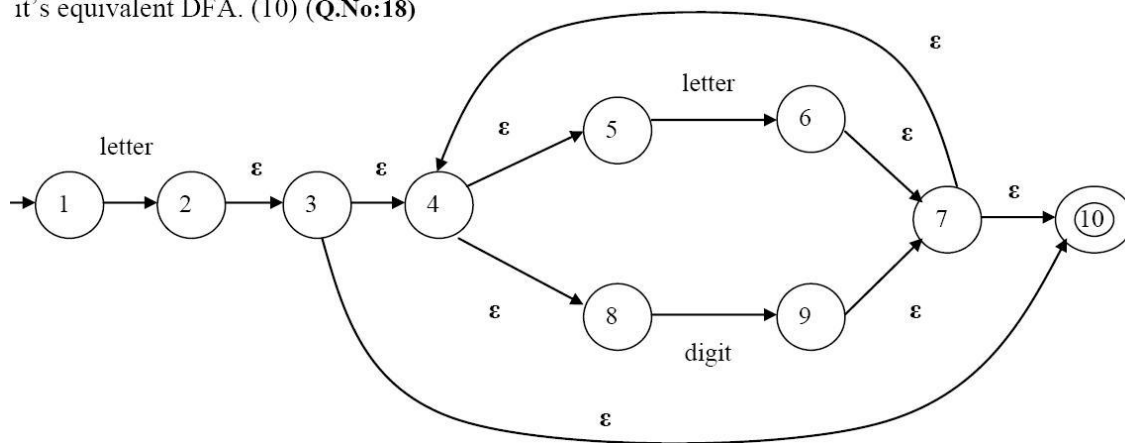
1.Explain inductive proof with example.(13)

2.Write about the various form of proof.(7)

3. Prove that “A language L is accepted by some DFA if and only if L is accepted by some NFA”(13)

4. consider the following ϵ -NFA for an identifier. Consider the ϵ -closure of each state and find it's equivalent DFA.(13) or (14)

it's equivalent DFA. (10) (Q.No:18)



5.convert the given NFA to DFA.(13)

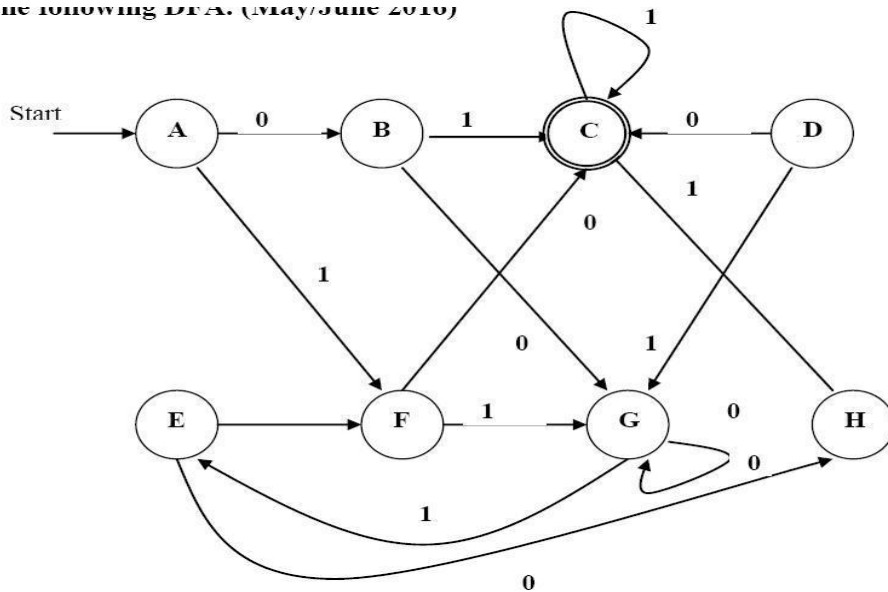
state/input	0	1
→ q0	{q0,q1}	q0
q1	q2	q1
q2	q3	q3
*q3	\varnothing	q2

6.Write any one example for NFA- ϵ to NFA without ϵ .(6)

7.Construct the minimal DFA for the regular expression $(b \setminus a)^*baa$.(13).

8. Write and explain the algorithm for minimization of a DFA. Using the above algorithm minimize the following DFA. (May/June 2016)(14)

the following DFA. (May/June 2010)



9.State pumping lemma with example.(13)

10.Describe the closure properties of regular languages. [APR/MAY 2018]

11.Determine DFA from a given NFA

$M = (\{q_0, q_1\}, \{0, 1\}, \delta, q_0, \{q_1\})$ where is given by

$\delta(q_0, 0) = \{q_0, q_1\}, \delta(q_0, 1) = \{q_1\}, \delta(q_1, 0) = \varnothing, \delta(q_1, 1) = \{q_0, q_1\}$ [APR/MAY 2018]

UNIT-II

GRAMMERS

PART-A

1. Define a Context Free Grammar. [**May/June 2010**]

2. What are the applications of Context free languages? [**Dec 2009**]

3. What is: (a) Derivation (b) Sub tree.

4. What is an ambiguous grammar? [**Dec 2009**]

5. Construct the grammar for the language $L = \{ a^n b^n \mid n \geq 1 \}$.

6. Construct the context-free grammar representing the set of palindromes over $(0+1)^*$ (Nov/Dec 2015)

7. Let the productions of a grammar be $S \rightarrow 0B, A \rightarrow 0S/1AA, B \rightarrow 1S/0BB$. For the string 0110 find a right most derivation. [**MAY/JUNE 2007**]

8. Construct a context free grammar for generating the language $L = \{ a^n b^n \mid n \geq 1 \}$ (Nov/Dec-2004, 2010, 2013, May-05, 06)

9. Convert the following grammar into an equivalent one with no unit productions and no useless symbols $S \rightarrow ABA, A \rightarrow aAA \mid aBC \mid bB, B \rightarrow A \mid bB \mid Cb, C \rightarrow CC \mid cC$.

(Nov/Dec 2011)

10. When a grammar is said to be ambiguous? (May 2013) [APR/MAY 2018]

11. Consider the following grammar G with productions (May 2010)

$S \rightarrow ABC \mid BaB$

$A \rightarrow aA \mid BaC \mid aaa$

$B \rightarrow bBb \mid a$

$C \rightarrow CA \mid AC.$

12. Let G be the grammar $S \rightarrow aB \mid bA$, $A \rightarrow a \mid aS \mid bAA$, $B \rightarrow b \mid bS \mid aBB$. For the string aaabbabbba find a leftmost derivation. (May/June'07)(Apr/May'08)(Nov/Dec 2015)

13. What do you mean by null production and unit production? Give an example.

14. Construct a CFG for set of strings that contain equal number of a's and b's over $\Sigma = \{a, b\}$ (May/June 2016)

15. What is meant by left and right sentential form?

16. Find the grammar for the language $L = \{a^n b c, \text{ where } n > 1\}$

17. Find the language generated by a CFG. $G = (\{S\}, \{0, 1\}, \{S \rightarrow 0/1/\epsilon, S \rightarrow 0S0/1S1/S\})$

18. Define Chomsky Normal Form? [APR/MAY 2018]

19. Derive the rules to remove ϵ productions with an suitable example (Dec'09)

20. Find the grammar for the language $L = \{a^n b c, \text{ where } n > 1\}$

PART-B

1) Derive the strings $a^*(a+b00)$ using leftmost and rightmost derivation for the following production. (8)

1. $E \rightarrow I$

2. $E \rightarrow E+E$

3. $E \rightarrow E * E$

4. $E \rightarrow (E)$

5. $I \rightarrow a$

6. $I \rightarrow b$

7. $I \rightarrow Ia$

8. $I \rightarrow Ib$

9. $I \rightarrow I0$

10. $I \rightarrow I1$

2. Show that the grammar $S \rightarrow aSbS \mid bSaS \mid \epsilon$ is ambiguous and what is the language generated by this grammar? (Nov/Dec 2006)(8)

3. The following grammar generates the language of Regular expression $0^*1(0+1)^*$.

$S \rightarrow A1B$

$A \rightarrow 0A \mid \epsilon$

$B \rightarrow 0B \mid 1B \mid \epsilon$

Give leftmost and rightmost derivations of the following strings

00101 b) 1001 c) 00011 (May/June 2006) (16)

4. Given the grammar $G = (V, \Sigma, R, E)$, where

$V = \{E, D, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, +, -, *, /, (,)\}$

$\Sigma = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 0, +, -, *, /, (,)\}$, and R contains the following rules:

$E \rightarrow D \mid (E) \mid E+E \mid E-E \mid E * E \mid E / E$

$$D \rightarrow 0 \mid 1 \mid 2 \mid \dots \mid 9$$

Find a parse tree for the string $1+2*3$. (6) (Nov/Dec 2015) (16)

5. Let G be the grammar $S \rightarrow 0B \mid 1A$, $A \rightarrow 0 \mid 0S \mid 1AA$, $B \rightarrow 1 \mid 1S \mid 0BB$.

For the string 00110101 find (Apr/May 2004) (May/Jun2007)(8)

6. Find the language $L(G)$ generated by the grammar G with variables S, A, B terminals a, b and productions $S \rightarrow aB$, $B \rightarrow b$, $B \rightarrow bA$, $A \rightarrow aB$.(8)

7. If G is a grammar $S \rightarrow SbS \mid a$ prove that G is ambiguous (Apr/May 2004)(8)

8. Show that the grammar $S \rightarrow a \mid Sa \mid bSS \mid SSb \mid SbS$ is ambiguous (8) (Nov/Dec2007)

9. Find a derivation tree of a^*b+a^*b given that a^*b+a^*b is in $L(G)$ where G is given by $S \rightarrow S+S/S^*S/a/b$ (May/June 2007).(8)

10. Let $G=(V,T,P,S)$ be a Context free Grammar then prove that if the recursive inference procedure tells us that terminal string W is in the language of variable A , then there is a parse tree with root A and yields w . (Nov/Dec 2015)(16)

11. Begin with the grammar

$$S \rightarrow ASB / \epsilon$$

$$A \rightarrow aAS/a$$

$$B \rightarrow SbS/A/bb$$

(a) Are there any useless symbols? Eliminate them

(b) Eliminate ϵ productions

(c) Eliminate unit productions

(d) Put the grammar into Chomsky normal form. (Nov/Dec 2015)(16) [APR/MAY

2018]

12. Find the CNF for the following grammar,

$$S \rightarrow aB/bA$$

$$A \rightarrow aS/bAA/a$$

$$B \rightarrow bS/aBB/b. \text{ (Nov/Dec 2005) (Nov/Dec 2006)}$$

13. What is the purpose of normalization? Construct the CNF and GNF for the following grammar and explain the steps. [APR/MAY 2018]

$$S \rightarrow aAa \mid bBb \mid \epsilon$$

$$A \rightarrow C \mid a$$

$$B \rightarrow C \mid b$$

$$C \rightarrow CDE \mid \epsilon$$

$$D \rightarrow A \mid B \mid ab \text{ (May/June 2016).}$$

14. Convert the following grammar to GNF

$$S \rightarrow AB$$

$$A \rightarrow BS/b$$

$$B \rightarrow SA/a.$$

UNIT-3

PUSH DOWN AUTOMATA

PART-A

1. Define Pushdown Automata. (May/June 2016)
2. What are the different types of language acceptances by a PDA and define them. (Nov/Dec 2015)
3. Define Deterministic PDA. [APR/MAY 2018]
4. Define Instantaneous description (ID) in PDA. (MAY-06/09)
5. How do you convert CFG to a PDA.
6. State the pumping lemma for CFLs.(May-08)
7. Convert the following CFG to a PDA (Nov/Dec 2015)
 - i. $S \rightarrow aAA, A \rightarrow aS \mid bS \mid a$
8. Does a pushdown Automata has memory? Justify. (May/June 2016)
9. Give an example of PDA.(DEC-05)
10. Is the language of DPDA and NPDA same? (MAY-06/09)
11. Define the languages generated by a PDA using the Two methods of accepting a language.(May-07)
12. Construct a PDA to accept a language $\{(an)^n \mid n \geq 1\}$ by empty stack.(Dec-09)
13. Compare NFA and PDA.(Dec-13)
14. Draw the symbols used in PDA.
15. Design PDA for the language $L=\{001\}$
16. Design PDA for the language $L=\{0011\}$
17. Define NDPDA.
18. What are the ways of language acceptance in PDA. [APR/MAY 2018].
19. Design DPDA for $L=a^n b^n$ where $n \geq 1$.
20. Write algorithm for getting production rule of CFG.

PART-B

INSTANTANEOUS DESCRIPTION:

- 1.Design PDA to accept the language $L=\{wcw^R \mid w=\{0,1\}^*\}$ (8) [APR/MAY 2018]
- 2.Design PDA for the language $L = \{anb2n \mid n \geq 0\}$ (Nov/Dec 2008) (8)
- 3.Construct a transition table for PDA which accepts the Language $L= \{ a3nbn \mid n \geq 0 \}$ (16)
- 4.Design a PDA to accept $\{0n 1n \mid n \geq 1\}$.Draw the transition diagram for the PDA. Show by instantaneous description that the PDA accepts the string '0011'. (10) (Nov/Dec 2015)(8)
- 5.Construct a pushdown automaton to accept the following language L on $\Sigma = \{a, b\}$ by empty stack $L= \{ ww^R \mid w \in \Sigma^+ \}$ (May/June 2016)(8)

Problems for converting PDA to CFG:

6. Convert the PDA $P = (\{q, P\}, \{0, 1\}, \{X, Z_0\}, \delta, q, z_0)$ to a CFG if δ is given by

- (a) $\delta(q, 1, z_0) = \{(q, Xz_0)\}$
- (b) $\delta(q, 1, X) = \{(q, XX)\}$
- (c) $\delta(q, 0, X) = \{(P, X)\}$
- (d) $\delta(q, \epsilon, X) = \{(q, \epsilon)\}$
- (e) $\delta(P, 1, X) = \{(P, \epsilon)\}$
- (f) $\delta(P, 0, z_0) = \{(q, z_0)\}$ (16)

7. Construct CFG for the following PDA where δ is given by,

$P = (\{q_0, q_1\}, \{0, 1\}, \{X, Z_0\}, \delta, q_0, z_0, \Phi)$

- (a) $\delta(q_0, 0, z_0) = \{(q_0, Xz_0)\}$
- (b) $\delta(q_0, 0, X) = \{(q_0, XX)\}$
- (c) $\delta(q_0, 1, X) = \{(q_1, \epsilon)\}$ (8) [APR/MAY 2018]

8. Convert PDA to CFG. PDA is given by $P = (\{p, q\}, \{0, 1\}, \{X, Z\}, \delta, q, Z)$, δ is defined by

- $\delta(p, 1, Z) = \{(p, XZ)\}$,
- $\delta(p, \epsilon, Z) = \{(p, \epsilon)\}$,
- $\delta(p, 1, X) = \{(p, XX)\}$,
- $\delta(q, 1, X) = \{(q, \epsilon)\}$,
- $\delta(p, 0, X) = \{(q, X)\}$,
- $\delta(q, 0, Z) = \{(p, Z)\}$, (Nov/Dec 2015) (16)

Converting CFG To PDA

9. Construct the PDA for the following grammar $E \rightarrow E+E \mid E * E \mid a$ (8)

10. Consider the grammar $G = (V, T, P, S)$ when $S \rightarrow aA$, $A \rightarrow aABC/bB/a$, $B \rightarrow b$, $C \rightarrow c$ and find the PDA. (8)

11. Construct the CFG for $L = \{0^n 10^n \mid n \geq 0\}$ and use it to construct PDA. (8)

DETERMINISTIC PUSHDOWN AUTOMATA

12. What are deterministic PDA's? Give example for Non-deterministic and deterministic PDA? (8) (Nov/Dec 2015)

PROBLEMS ON PUMPING LEMMA

13. State pumping Lemma for CFL. Use pumping lemma to show that the language $L = \{a^i b^j c^k \mid i < j < k\}$ is not a CFL. (8) [APR/MAY 2018]

14. Show that the language $L = \{a^n b^n c^n \mid n \geq 0\}$ is not a context free language. (8) [APR/MAY 2018]

UNIT-4

TURING MACHINE

PART-A

1. What is a Turing Machine? (MAY/JUNE-16) [APR/MAY 2018]

2. What is a multitape Turing machine?(NOV/DEC-15)
3. Write about the chomskian hierarchy of languages.(APR/MAY-17) [APR/MAY 2018]
4. What is halting problem?(APR/MAY-17)
5. Define instantaneous description and move of a turing machine.
6. what are the features of universal turing machine?
7. What is meant by multihead turing machine?
8. What are the applications of Turing machine? (Dec-12)
9. List out techniques for Turing machine construction.(Dec -13)
10. What are the possibilities of a TM when processing an input string?
11. What are the techniques for Turing machine construction?
12. Differentiate Multitape and Multitrack machines.(Dec-08)
13. When is checking off symbols used in TM?
14. What is a 2-way infinite tape TM?
15. What are the reasons for a TM not accepting its input?
16. Construct a Turing machine to compute 'n mod 2' where n is represented in the tape in unary form consisting of only 0's. (May – 11)
17. Design a Turing machine with not more than states that accepts languages $a(a+b)^*$. Assume $\Sigma = \{a, b\}$ (May-05).
18. What are the Comparison of FM, PDA and TM?
19. Define Power of turing Machine.
20. What are the differences between a finite automata and a Turing machine?(APR/MAY-16)

PART-B

TURING MACHINE

- 1.Explain the programming techniques for Turing Machine construction. (14)(Nov/ Dec-12)(13)
- 2.Explain briefly about Two way Turing Machine.(7) (May/June-04,05, Nov/Dec-05,08,09,12,13)

COMPUTATIONAL LANGUAGES AND FUNCTIONS

- 3.Construct TM for the language $L = \{a^n b^n\}$ where $n \geq 1$. (May – 09)(7)
- 4.Construct a TM for $L = \{1^n 0^n 1^n / n \geq 0\}$.(May – 12)(6)
- 5.Construct TM for performing subtraction of two unary numbers $f(a-b) = c$ where a is always greater than b.(Dec -03,Dec – 05,May -11)(7)

TWO WAY TURING MACHINE

- 6.Construct a TM for a language having equal number of a's and b's.(7)
- 7.Construct a TM for a language obtaining two's complement of a binary number.(7)
- 8.Construct a TM for reversing a binary string on the input tape.(6)
- 9.Build a multitrack turing machine for checking whether given number is prime or not?(7)
- 10.Design a turing machine which reverses the given string{abb}.(6) [APR/MAY 2018]

TYPES OF TURING MACHINE

- 11.Explain about Types of Turing machine.(7)

HALTING PROBLEM

- 12.Explain Halting problem. Is it solvable or unsolvable problem? Discuss.(13) (May/June-16)

CHOMSKY HIERARCHY OF LANGUAGES

13.Explain about the Chomsky hierarchy of languages.(DEC-15)(7)

14.construct Turing machine perform unary multiplication. [APR/MAY 2018]

UNIT-5

UNSOLVABLE PROBLEMS AND COMPUTABLE FUNCTIONS

PART-A

1. When a problem is said to be decidable and give an example of undecidable problem. (Nov/Dec 2015)
2. Show that the complement of a recursive language is recursive.(Dec-04,may-05)
3. Give two properties of Recursively Enumerable Sets which are undecidable.
4. When a language is said to be recursive? Is it true that every regular set is not recursive?(Nov/Dec -05)
5. Differentiate between recursive and recursively enumerable languages.(Apr/May-07)
6. When do you say a problem is NP-hard?(Dec-09)
7. Mention the difference between P and NP problems.
8. What is recursively enumerable? (May-12,Nov/Dec-13) [APR/MAY 2018]
9. Show the union of recursive language is recursive.
10. What are a) Recursively Enumerable b) Recursive sets? (Nov/Dec-13)
11. Define the class NP problem.(Nov/Dec-13)
12. What do you mean by universal turing machine?(Nov/Dec-05,13)
13. Define the classes P and NP problems. (May-14)
14. When a recursively enumerable language is said to be recursive? Is it true that the language accepted by a non-deterministic Turing machine is different from recursively enumerable language? (May/June 2016)
15. What are the different types of grammars/languages?
16. Define PCP or Post Correspondence Problem?
17. Define MPCP or Modified PCP.
18. What is a universal language L_u ? (Nov/Dec 2015) [APR/MAY 2018]
19. Define Rice Theorem?
20. What is primitive recursive function?(May-2017)

PART-B

1. (i) Prove that “MPCP reduces to PCP”. (10) (Nov/Dec 2015)
(ii) Discuss about the tractable and intractable problems. (6) (Nov/Dec 2015)

2. (i) State and explain RICE theorem. (10) **(Nov/Dec 2015)**
(ii) Describe about Recursive and Recursively Enumerable languages with examples.
(6)
3. What is a universal Turing machine? Bring out its significance. Also construct a Turing machine to add two numbers and encode it. (16) **(May/June 2016)**
4. What is a post corresponding problem (PCP)? Explain with the help of an example.(10) **(May/June 2016)**
- 5.Explain recursive and recursive enumerable language with suitable example.(16) (May-2017)
- 6.Explain Tractable and intractable problems with suitable example.(16) (May-2017)
- 7.Describe about the Universal TM.(7)
- 8.rite notes on primitive recursive function. [APR/MAY 2018]
- 9.Write note on NP complete problem and polynomial time reduction. [APR/MAY 2018]